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Synthesis and thermoelectric properties of Re₃As_{6.6}In_{0.4} with Ir₃Ge₇ crystal structure

Valeriy Y. Verchenko¹, Anton S. Vasiliev¹, Alexander A. Tsirlin², Vladimir A. Kulbachinskii³, Vladimir G. Kytin³ and Andrei V. Shevelkov^{*1,§}

Full Research Paper

Address:

¹Department of Chemistry, Lomonosov Moscow State University, Moscow 119991, Russia, ²National Institute of Chemical Physics and Biophysics, 12618 Tallinn, Estonia and ³Faculty of Physics, Lomonosov Moscow State University, Moscow 119991, Russia

Email:

Andrei V. Shevelkov* - shev@inorg.chem.msu.ru

* Corresponding author § Fax: +7 495 939 4788.

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Abstract

The Re₃As_{7-x}In_x solid solution was prepared for $x \le 0.5$ by heating the elements in stoichiometric ratios in evacuated silica tubes at 1073 K. It crystallizes with the Ir₃Ge₇ crystal structure, space group Im-3m, with a unit-cell parameter a ranging from 8.716 to 8.747 Å. The crystal structure and properties were investigated for a composition with x = 0.4. It is shown that indium substitutes arsenic exclusively at one crystallographic site, such that the As-As dumbbells with $d_{As-As} = 2.54$ Å remain intact. Re₃As_{6.6}In_{0.4} behaves as a bad metal or heavily doped semiconductor, with electrons being the dominant charge carriers. It possesses high values of Seebeck coefficient and low thermal conductivity, but relatively low electrical conductivity, which leads to rather low values of the thermoelectric figure of merit.

Introduction

Thermoelectric materials with good efficiency are highly awaited by modern power engineering. Utilizing either the Seebeck or Peltier effects, it is possible to produce electricity from waste heat (e.g., that stemming from combustion in car engines) or to cool an environment under an external power supply. However, the efficiency of these processes depends on

the efficiency of the thermoelectric material in question, which is defined by the value of the figure of merit $ZT = TS^2\sigma/\kappa$, where T is the absolute temperature, S the Seebeck coefficient, σ the electrical conductivity, and κ the thermal conductivity. It is shown in the literature [1] that the best thermoelectric materials are to be sought among narrow-gap semiconductors

composed of heavy elements, in which structural features favor low thermal conductivity [2]. Attempts to improve the ZT value have led to the investigation of various types of thermoelectrics beyond the long-known lead and bismuth tellurides [3,4]. Among new candidates are the filled skutterudites [5,6], semiconducting clathrates [7], disordered materials such as Zn_4Sb_3 [8], and various inorganic and intermetallic compounds with complex crystal structures [9,10]. Compounds with the Ir_3Ge_7 structure type, namely $Mo_3Sb_{5+\delta}Te_{2-\delta}$ [11], $Nb_3Sb_2Te_5$ [12] and $Re_3As_{7-x}Ge_x$ [13], belong to the latter type of potential thermoelectric materials and have recently shown promising ZT values.

All members of the Ir₃Ge₇ family crystallize in the cubic space group Im-3m and feature the M-M dumbbells inside the Archimedean antiprism of the non-transition-element atoms. The strong hybridization of the transition-metal d-orbitals with the p-orbitals of a non-transition element may lead to the opening of a band gap near the Fermi level [14]. As a result, compounds with 55 valence electrons per formula unit (f.u.) exhibit semiconductor-like behavior. The number of valence electrons can be tuned through the solid-solution formation. For instance, Mo₃Sb₅Te₂ and Re₃As₆Ge adopt 55 e^- per f.u. and should be semiconductors according to the band structure calculations. Their doped analogues, Mo₃Sb_{5.4}Te_{1.6} and Re₃As_{6.4}Ge_{0.6}, display minor deviation from $55 e^-$ per formula. They behave as heavily doped semiconductors and possess the ZT values of 0.8 at 1050 K and 0.3 at 700 K, respectively [13]. To expand the Ir₃Ge₇ family and search for new promising thermoelectrics, we investigated different ways of obtaining new solid solutions based on Re₃As₇ or Mo₃Sb₇ compounds. In this paper, we report on the synthesis of the Re₃As_{7-x}In_x solid solution ($x \le 0.5$), its crystal and electronic structures, and its thermoelectric properties.

Experimental

Synthesis and analysis

Rhenium (-325 mesh, 99.99%, Alfa Aesar) and arsenic (-70 mesh, 99.99%, Alfa Aesar) powders and indium ingots (99.95%, Sigma Aldrich) were used as received. Phase purity of the starting materials was checked by using the standard X-ray diffraction technique, and in all cases no impurity phases were found. To synthesize the title solid solution, stoichiometric quantities of the starting elements were heated in evacuated silica tubes at 1073 K for 7 days with further cooling to room temperature in a shut off furnace. Firstly, the samples were analyzed by means of X-ray powder diffraction using a Stoe STADI-IP diffractometer with Cu Ka₁ radiation (Ge monochromator, $\lambda = 1.540598$ Å). To evaluate the lattice constants of the Re₃As_{7-x}In_x solid solution, all X-ray diffraction patterns were recorded with Ge as an internal standard (a = 5.6576 Å). The data were treated with the program package Stoe WinXPOW. Secondly, the obtained samples were analyzed with a JSM JEOL scanning electron microscope operated at 20 kV and equipped with an EDX detection system INCA x-Sight. Both point-spectra acquisition and element mapping were used to investigate the elemental and phase composition of the samples.

Structure determination

The crystal structure was determined by the Rietveld method from the X-ray powder diffraction data. For the sample with the nominal composition $Re_3As_{6.6}In_{0.4}$, hereafter sample S1, the data were recorded with the Bruker D8 Advance diffractometer, Cu $K\alpha_1$ radiation (Ge monochromator, $\lambda = 1.540598$ Å). For the Rietveld refinements we used the TOPAS software (version 4.2, Bruker-AXS). The refinement enabled us to determine minor quantities of three impurity phases (Table 1) that were taken into account during the subsequent refinement. The atomic parameters taken from the crystal structure of Re_3As_7 [15] were

refined composition	$Re_3As_{6.70(3)}In_{0.30(3)}$		
formula weight (g⋅mol ⁻¹)	1095.041		
T (K)	300		
wavelength (Å)	1.540598		
space group	<i>lm</i> −3 <i>m</i> (No. 229)		
cell dimensions, a (Å)	8.74231(6)		
<i>V</i> (Å ³)	668.157(14)		
no. of formula units per cell	4		
calculated density (g⋅cm ⁻³)	10.88		
2θ range (°)	17.00–85.01		
$R_{\rm p}, R_{ m wp},$ GOF	0.056, 0.077, 1.4		
impurity phases (weight %)	Re 2.0%, InAs 2.3%, In ₂ O ₃ 1.0%		

Table 2: A	tomic coordina	tes and displacemer	nt parameters for S1 .			
site	Wyck.	X	У	z	$B_{\rm iso}({\rm \AA}^2)$	occupancy
Re	12e	0.3396(2)	0	0	0.60(3)	1Re
E1	12d	1/4	0	1/2	0.82(11)	0.90(1)As + 0.10(1)In
As2	16f	0.1662(2)	0.1662(2)	0.1662(2)	0.82(5)	1As

used as the starting model. The refinement showed that the unique position of the rhenium atom was fully occupied. One of the two positions of the arsenic atoms, namely, the 12d site, showed a remarkably low atomic displacement parameter and was subsequently refined as jointly occupied by indium and arsenic. The refinement led to the composition Re₃As_{6.70(3)}In_{0.30(3)} in reasonable agreement with the starting (synthetic) composition. Crystallographic details of the refinement are shown in Table 1, and the atomic parameters are shown in Table 2. Selected interatomic distances are listed in Table 3.

mic distances for S1 .	
distance (Å)	
2.597(1)	
2.553(1)	
2.805(3)	
2.539(5)	
2.905(3)	
	distance (Å) 2.597(1) 2.553(1) 2.805(3) 2.539(5)

Electronic-structure calculations

The FPLO (full potential local orbitals) code was utilized for the electronic-structure calculations [16]. FPLO performs density functional calculations with the local density approximation (LDA) for the exchange–correlation potential [17]. The crystallographic data presented in Table 4 were used for the calculations [15]. The integrations in the k space were performed by an improved tetrahedron method [18] on a grid of $16 \times 16 \times 16$ k points evenly spread in the first Brillouin zone.

Table 4: Re₃As₇ crystallographic data used for electronic-structure Space group Im-3m (No. 229), a = 8.7162(7) Å site Wyck. z 0 Re 12e 0.3406(9)0 As1 12d 1/4 1/2 As2 16f 0.1687(20) 0.1687(20) 0.1687(20)

Physical property measurements

For thermal transport measurements, the sample S1 was thoroughly ground and pressed at room temperature into a rectangular pellet of dimensions $8 \times 3 \times 2 \text{ mm}^3$. The density of S1 was estimated from the linear sizes of the pellet to be about 70% of the theoretical density. This pellet was used to measure the electrical conductivity (σ) , the Seebeck coefficient (S), and the thermal conductivity (κ) in the temperature range of 77-300 K in a home-built setup. Resistance was determined from the voltage drops by applying a four-probe method in accordance with Ohm's law, i.e., $R = \Delta V/I$. The current (I) was scanned in the range between 2.5 µA and 16 mA, and subsequently σ was calculated after measuring the length between the contacts (L) according to $\sigma = L/(AR)$, with the area A = $3 \times 2 \text{ mm}^2$. The Seebeck coefficient and thermal conductivity were measured by using an internal standard to determine the temperature difference in a custom-designed sample puck that was plugged into the cold finger of a closed-cycle refrigerator. All measurements were performed under dynamic vacuum.

For the magnetization measurements, powder samples of Re₃As₇ and S1 were loaded into plastic capsules. Measurements were performed with the VSM setup of Quantum Design PPMS in external fields of 0.1, 0.5, 1, 2, and 5 T. To estimate the diamagnetic contribution from the sample holder, an empty capsule was measured under the same conditions.

Results and Discussion Synthesis, sample characterization and crystal structure

The synthesis of the $Re_3As_{7-x}In_x$ series with x=0, 0.2, 0.4, 0.6, 0.8, and 1 from pure elements resulted in black powders that were stable in air. The obtained samples were analyzed by X-ray powder diffraction. All samples showed reflections of the main phase of the Re_3As_7 type (space group Im-3m), together with minor reflections of Re, InAs, and In_2O_3 admixtures, the presence of which was also confirmed with EPMA (Figure 1). In order to obtain single-phase samples, we tried to improve the synthetic procedure, but neither increasing the annealing time nor pressing the reactants into pellets led to phase-pure samples. Some general trends should be noted. For the samples with $0 \le x \le 0.4$, absolute intensities and, thus, quantities of admixtures remain constant, while for x > 0.5, quantities of Re and

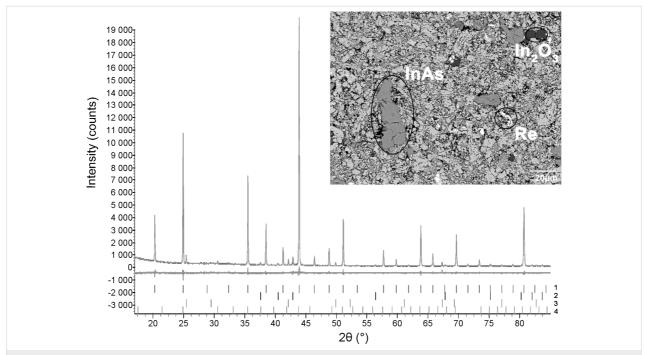


Figure 1: The plot of Rietveld refinement for the **S1** sample. Experimental and difference curves, and positions of Bragg peaks are shown on the plot. Marked with numbers: 1: Re₃As_{6.70(3})In_{0.30(3)}; 2: Re; 3: InAs; 4: In₂O₃. Inset: SEM micrograph of **S1** showing the distribution of secondary phases in the microstructure (the most contaminated portion was chosen for showing all three admixtures).

InAs start to increase. Additionally, we found by a linear interpolation that the unit cell parameter of the Re₃As_{7-x}In_x solid solution increases up to x = 0.5, and then remains constant at higher x (Figure 2). All these facts suggest that the solid solution in question exists only for $x \le 0.5$. The outermost composition Re₃As_{6.5}In_{0.5} possesses exactly 55 valence electrons per formula unit. As mentioned above, this electron concentration should yield the semiconducting behavior for compounds with

the Ir₃Ge₇ structure type. Thus, the indium substitution for arsenic in Re₃As₇ could be used as a chemical modification to control transport properties of this system.

The crystal structure of the solid solution was studied for the S1 sample by the Rietveld method from X-ray powder diffraction data (Figure 1, Table 1 and Table 2). The title compound crystallizes with the Ir₃Ge₇ crystal structure (Figure 3). This structure

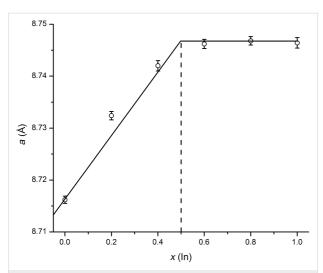


Figure 2: Dependence of the $\text{Re}_3\text{As}_{7-\chi}\text{ln}_\chi$ cubic-unit-cell parameter on the nominal indium content. Esd's are calculated from least-squares fits of the powder data.

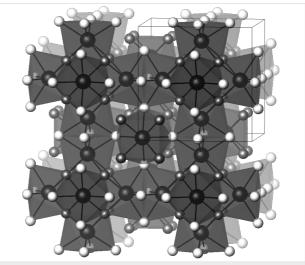


Figure 3: Polyhedral view of the $Re_3As_{7-x}In_x$ crystal structure. Re is shown as black spheres inside the polyhedra, E1: white spheres, and As2: gray spheres at the vertices.

ture can be described as being composed of rhenium-centered square antiprisms of E atoms, ReE_8 (E = As/In). Two square antiprisms are linked by sharing a square face. These pairs form the so-called Re_2E_{12} barrels, the main building blocks of the crystal structure. The barrels, oriented along the main crystallographic directions, form two interpenetrating 3D networks in accordance with the body-centering and, thus, build up the entire crystal structure.

The formation of the solid solution may be associated with a chemical substitution on different crystallographic sites. There are two sites forming the coordination polyhedra of E atoms in the Ir₃Ge₇ structure type (Figure 4), and the substitution is possible for both sites depending on the chemical nature of the E elements. It is known from the literature that in the case of the Ge for As substitution in the parent compound Re₃As₇, all Ge atoms enter the As2 (16f) site [13]. In contrast, we have found that when indium substitutes for arsenic in Re₃As₇, all indium atoms are on the E1 (12d) site. The preference for the certain As position depends on different aspects, including size, nuclear charge, and number of valence electrons of the heteroatom. In particular, there is an E-E single bond between atoms occupying the 16f site, with a bond distance of 2.538(5) Å. Clearly, indium does not favor such a short bond to arsenic and, therefore, avoids the occupation of this site.

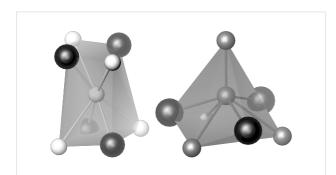


Figure 4: Coordination polyhedra of E1 (left) and As2 (right) sites in the crystal structure of Re₃As_{7-x}In_x.

Electronic structure, magnetic and thermoelectric properties

The computed density of states for Re₃As₇ is shown in Figure 5. The Fermi level lies slightly above the gap of 0.8 eV that separates the conduction band from the valence band. The nonzero DOS at $E_{\rm F}$ implies metallic behavior for the undoped Re₃As₇. Additionally, the steep slope of the DOS curve near $E_{\rm F}$ should lead to a high Seebeck coefficient according to $S \sim 1/N \cdot \partial N(E_{\rm F})/\partial E$ [19], provided that the system is made semiconducting by doping. Indeed, the absolute values of S for Re₃As_{6.4}Ge_{0.6} exceed 150 μ V·K⁻¹ at high temperatures, thus leading to high values of S [13].

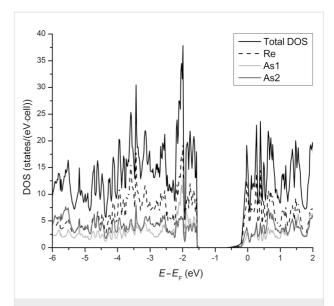


Figure 5: Density-of-states curve for Re₃As₇. Re contribution: dashed line, As1 and As2: light and dark gray lines, respectively.

In Re₃As₇, the calculated density of states at $E=E_{\rm F}$ is 8.3 states/(eV·f.u.). For the solid solution Re₃As_{6.7}In_{0.3} (the composition obtained from the Rietveld refinement of the X-ray powder diffraction data, see Table 1), the DOS is reduced to 5.15 states/(eV·f.u.), given the rigid-band shift with the assumption that Re₃As₇ possesses 56 valence electrons per f.u. and Re₃As_{6.7}In_{0.3} 55.4 electrons. Therefore, both compounds should be metallic with a Pauli paramagnetic contribution to the total susceptibility $\chi = \chi_{dia} + \chi_{\rm P}$, where χ_{dia} is core diamagnetism, and $\chi_{\rm P} = \mu_{\rm B}^2 \cdot N(E_{\rm F})$, with $\mu_{\rm B}$ being the Bohr magneton [20]. The formula yields $\chi_{\rm P} = 9 \times 10^{-5}$ and 5.5 × 10⁻⁵ emu/mol for Re₃As₇ and S1, respectively.

Experimentally, both Re₃As₇ and S1 show substantial diamagnetism in the examined temperature range. However, the susceptibility curves, Figure 6, lie above the level of core diamagnetism $\chi_{dia} = -3.37 \times 10^{-4}$ emu/mol, computed for a combination of Re⁷⁺ and As(V) [21]. Therefore, both pure and In-doped Re₃As₇ feature an additional paramagnetic contribution to the susceptibility. The experimental value of χ_P = $\chi - \chi_{dia} = 1.20(7) \times 10^{-4}$ emu/mol for Re₃As₇ is reasonably close to the one expected from the DOS at $E_{\rm F}$. However, the calculation of χ_P substantially depends on the estimation method of χ_{dia} , especially for a compound that cannot be considered as ionic. For this reason, the calculated value of χ_P may differ from the experimental one. The susceptibility of the S1 slightly decreases upon cooling but starts increasing below 80 K. While the low-temperature upturn could be due to a small number of paramagnetic impurities, the conspicuous increase in χ above 80 K does not conform to the Pauli paramagnetism and reflects deviations of S1 from a simple metal.

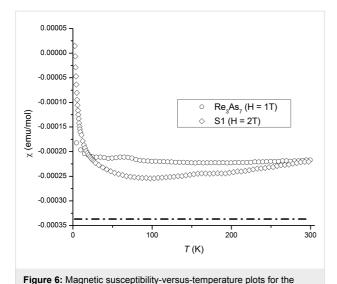


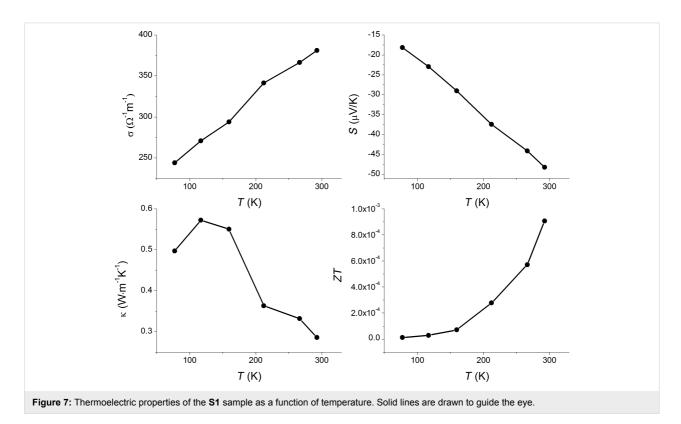
Figure 7 compiles the plots of the electric conductivity (σ) , Seebeck coefficient (S), thermal conductivity (κ) , and ZT in the temperature range of 77–300 K for S1. S is negative in this temperature range, evidencing that the S1 is an n-type conductor. However, the σ -versus-T behavior for the S1 sample is neither metallic nor classically semiconducting, because σ increases almost linearly with temperature. Thus, S1 can be regarded as a bad metal or degenerate semiconductor, consid-

Re₃As₇ and **S1** samples. The contribution of core diamagnetism is

shown as a dash-dotted line.

ering the possible presence of defects, such as vacancies in its crystal structure, which was proposed earlier for Re₃As₇ [15]. In the Ir₃Ge₇ family, Re₃As_{7-x}Ge_x exhibits n-type conductivity [13], while Mo₃Sb_{5+δ}Te_{2-δ} is a p-type conductor [11]. The obtained values of S for **S1** are comparable with those for Re₃As_{6.4}Ge_{0.6} and Mo₃Sb_{5.4}Te_{1.6}: -49, -72, and +55 μ V·K⁻¹ at 300 K, respectively [11,13]. Moreover, the extent of the substitution x in the Re₃As_{7-x}In_x solid solution can be further optimized, and possibly lead to larger values of S. Unfortunately, the **S1** displays considerably lower values of the electrical conductivity compared to both Re₃As_{7-x}Ge_x and Re₃As_{7-x}Sn_x (0.1 $\leq x \leq$ 0.6) [22]. For instance, the room-temperature value of 1090 Ω ⁻¹·cm⁻¹ for Re₃As_{6.4}Ge_{0.6} [13] is about 3000 times larger than the observed value of 3.8 Ω ⁻¹·cm⁻¹ for **S1**.

The thermal conductivity of the sample S1 is quite low. Its room-temperature value is $0.3~W \cdot m^{-1} \cdot K^{-1}$, which is an order of magnitude lower than for the Ge- and Sn-substituted compounds. This may be caused by two factors: Firstly, it could be attributed to the preference of indium atoms for only one position within the crystal structure (increased structural complexity); secondly, relatively low density of the sample (about 70%) may diminish the thermal conductivity due to the sample porosity. The total thermal conductivity is a sum of the electronic (κ_e) and lattice (κ_L) parts. Taking into account the rather low electrical conductivity and applying the



Wiedemann–Franz relation $\kappa_e = \sigma LT$, where L is the ideal Lorentz number, we estimate that the electronic part of the total thermal conductivity is negligibly small, and the observed value is essentially the lattice contribution to the thermal conductivity.

Combining the electrical conductivity, Seebeck coefficient and thermal conductivity, we calculate the temperature dependence of ZT shown in Figure 7. ZT increases with temperature, and reaches ZT = 0.0008 at room temperature, which is 30 times lower than for $Re_3As_{7-x}Ge_x$ [13]. Given the compositional width of the $Re_3As_{7-x}In_x$ solid solution and the low thermal conductivity of the investigated sample, we note that the optimum combination of S and σ for $Re_3As_{7-x}In_x$ is still to be found.

Conclusion

Chemical modification of Re_3As_7 resulted in the formation of the new Re_3As_7 -based solid solution $Re_3As_{7-x}In_x$ ($x \le 0.5$) with an Ir_3Ge_7 type of crystal structure. The indium for arsenic substitution occurs exclusively on the 12d site, thus keeping intact the As–As dumbbells with $d_{As-As} = 2.538(5)$ Å. While Re_3As_7 shows a Pauli paramagnetic contribution to the magnetic susceptibility in line with the results of band-structure calculations, the **S1** sample behaves as a bad metal or heavily doped semiconductor, with electrons being the dominant charge carriers. This compound combines low thermal conductivity with a relatively low electrical conductivity, and therefore, its thermoelectric figure of merit ZT reaches only 0.0008 at room temperature. Further optimization of the thermoelectric properties by varying the chemical composition of $Re_3As_{7-x}In_x$ is proposed.

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