



# Fingerprints of a size-dependent crossover in the dimensionality of electronic conduction in Au-seeded Ge nanowires

Maria Kolešnik-Gray<sup>1</sup>, Gillian Collins<sup>2</sup>, Justin D. Holmes<sup>2</sup> and Vojislav Krstić<sup>\*1</sup>

## Letter

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### Address:

<sup>1</sup>Department of Physics, Friedrich-Alexander-University Erlangen-Nürnberg (FAU), Staudtstr. 7, 91058 Erlangen, Germany and <sup>2</sup>Materials Chemistry & Analysis Group, Department of Chemistry, University College Cork, Cork, Republic of Ireland

### Email:

Vojislav Krstić\* - vojislav.krstic@fau.de

\* Corresponding author

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## Abstract

We studied the electrical transport properties of Au-seeded germanium nanowires with radii ranging from 11 to 80 nm at ambient conditions. We found a non-trivial dependence of the electrical conductivity, mobility and carrier density on the radius size. In particular, two regimes were identified for large (lightly doped) and small (stronger doped) nanowires in which the charge-carrier drift is dominated by electron-phonon and ionized-impurity scattering, respectively. This goes in hand with the finding that the electrostatic properties for radii below ca. 37 nm have quasi one-dimensional character as reflected by the extracted screening lengths.

## Results and Discussion

Synthetic germanium nanowires (Ge NWs) have been proposed as potential next-generation components for high-performance applications [1-3]. Besides representing prospective field-effect devices [4,5], they have attracted interest as building blocks for nanoscaled electrooptical components [6] and, due to their specific surface properties [4] can be envisaged as high-potential chemical and biological sensors as discussed for other types of semiconductor NWs [7-10].

Successful implementation of NWs into the aforementioned sensor technologies requires an optimized operation regime

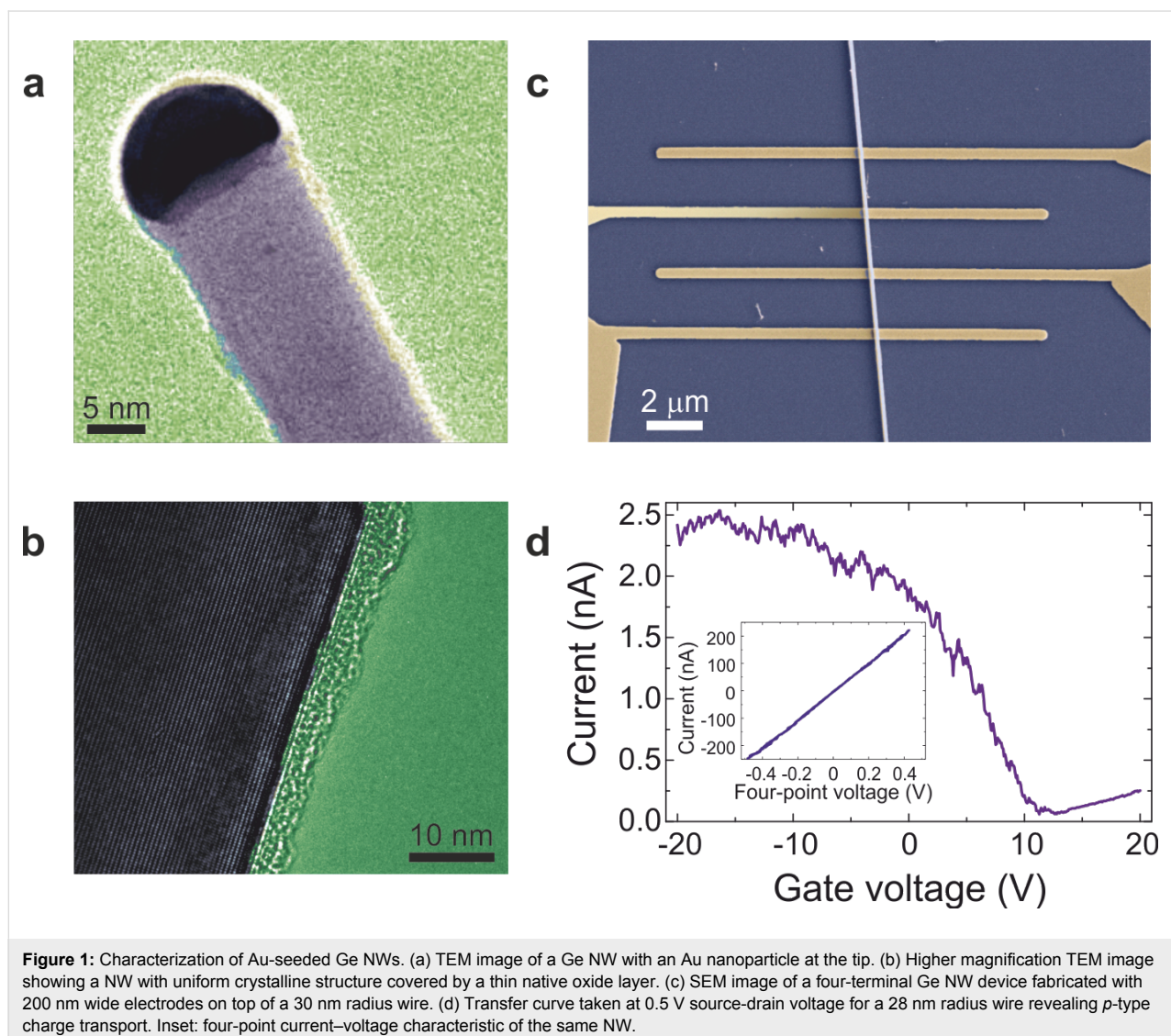
which will depend on the dimensionality of the electronic system. In particular, to ensure a significant electronic response to changes at the NW surface region, both the electrostatic screening length should be larger than the NW radius and the surface-to-volume ratio maximised [8]. This in turn will only be fulfilled for a certain range of screening lengths [7] and associated NW surface-to-volume ratios [8]. While the surface-to-volume ratio scales with NW radius and therefore can be controlled by adjusting synthesis conditions [11,12], the screening length depends on the density and dimensional character of the charge carriers in the NW [8]. Therefore it is crucial to investi-

gate the charge transport properties in the NWs of choice as function of their radius  $R$  to identify their different operation regimes.

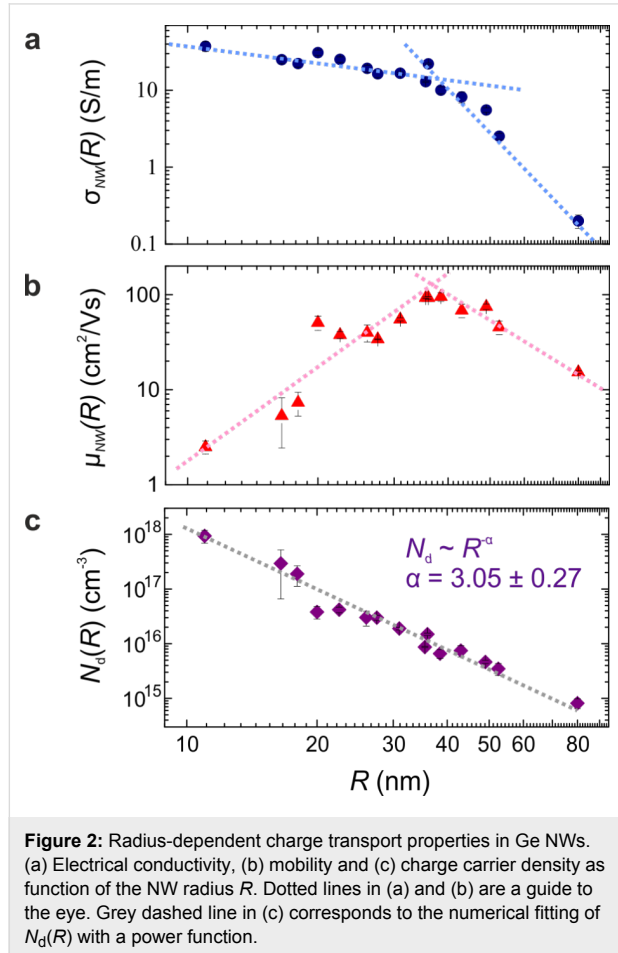
To this end, we carried out electrical characterization at ambient conditions of individual Au-seeded Ge NWs with  $R$  ranging from 11 to 80 nm (cf. Supporting Information File 1). By experimentally measuring the electrical conductivity,  $\sigma_{\text{NW}}$ , and field effect mobility,  $\mu_{\text{NW}}$ , we were able to identify the dominant scattering mechanisms and the  $R$ -dependence of the electrostatic screening length.

Ge NWs used in this study were synthesized at 400 °C on anodized alumina supports using a Au nanoparticle seeded vapour-liquid-solid process [13]. TEM analysis revealed that the NWs are monocrystalline with uniform radius along the axis (Figure 1a), have predominant  $\langle 110 \rangle$  growth direction and are

covered with a thin native oxide layer (Figure 1b). Individual NWs were deposited on degenerately doped Si substrates with 300 nm thermally grown  $\text{SiO}_2$  on top and contacted lithographically with Ag electrodes [14] in a four-point-probe configuration (Figure 1c). The Si backside of the chip was used as global backgate. For each NW, four-point current–voltage and transfer characteristics were taken under ambient conditions. All NWs showed  $p$ -type transfer characteristics (Figure 1d) indicating that the majority charge carriers are holes (cf. Supporting Information File 1) which is consistent with the existing studies on similar VLS grown semiconducting NWs [15–17]. In particular, the doping in our NWs is predominantly through surface states (cf. Supporting Information File 1). Also, our previous work [14] showed that the carrier-distribution is uniform over length scales of several hundred nm's along each NW unlike potentially expected for deliberately volume-doped Si NWs [18–21].



From the measured data,  $\sigma_{\text{NW}}$ ,  $\mu_{\text{NW}}$  and the carrier density,  $N_d$ , values were extracted and are plotted in Figure 2 as function of the NW radius  $R$ .

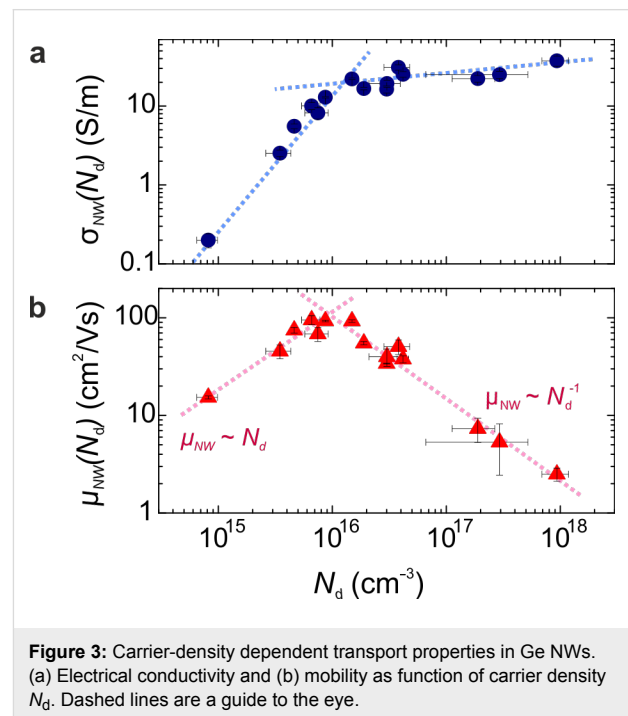


$\sigma_{\text{NW}}(R)$  showed a monotonous decrease by two orders of magnitude with increasing NW radius (Figure 2a). A change in the  $R$ -dependence was observed at about 36 to 37 nm. Notably, for the same  $R$  we find a maximum in the  $\mu_{\text{NW}}(R)$  (Figure 2b). This qualitative change in the  $R$ -dependence for both  $\sigma_{\text{NW}}(R)$  and  $\mu_{\text{NW}}(R)$  suggests a crossover in charge-carrier conduction. We note that the data in Figure 2a also confirms that surface-scattering is negligible at these radii, as the conductivity increases by orders of magnitude with radius reduction (an opposite dependence would have been expected otherwise).

To provide insight into the nature of this crossover, we first extract  $N_d(R)$  (cf. Supporting Information File 1) which is shown in Figure 2c. The measured carrier density in all cases exceeds the intrinsic doping level of bulk Ge ( $1.3 \times 10^{13} \text{ cm}^{-3}$  [22]), which indicates that the carrier-concentration is equivalent to the number density of ionized acceptor levels (surface-dopant concentration). Numerical fitting revealed

$N_d(R) \sim R^{-\alpha}$  with  $\alpha = 3.05 \pm 0.37$  showing that large radius NWs are comparably lightly doped. We note that the carrier concentration in the NW depends on the surface-state density which can vary depending on the synthesis conditions [15,23,24]. Therefore, the radius dependence of the carrier concentration may vary in differently grown NWs.

Since we found a non-trivial  $N_d(R)$  dependence, it is instructive to graph the conductivity and mobility as a function of carrier density, as is shown in Figure 3.



For low dopant densities,  $\sigma_{\text{NW}}(N_d)$  first increases by two orders of magnitude, and for  $N_d$  exceeding  $\approx 10^{16} \text{ cm}^{-3}$  it enters into a slowly varying regime (Figure 3a). In the case of mobility (Figure 3b), between  $\leq 10^{15}$  and  $\approx 10^{16} \text{ cm}^{-3}$   $\mu_{\text{NW}}(N_d) \approx N_d$ , indicating that lattice phonon scattering is the main mechanism limiting the carrier drift [25]. The dominance of electron phonon scattering within this density range suggests that the free holes behave similar to those in ( $p$ -type) bulk Ge [18]. For higher  $N_d$ , however,  $\mu_{\text{NW}}(N_d) \sim N_d^{-1}$  which is characteristic of ionized impurities being the dominant scatterers [25]. This coincides with the slow-varying region in  $\sigma_{\text{NW}}(N_d)$  which indicates that a further augmentation in  $\sigma_{\text{NW}}(N_d)$  is inhibited due to the increased density of scattering centres which counterbalances the increasing  $N_d$ . Remarkably, in bulk  $p$ -Ge ionized impurity scattering is expected to contribute significantly over our entire experimental carrier-density range [22,25,26], which would, in contrast to our data, lead to a rather flat  $N_d$  dependence up to  $10^{16} \text{ cm}^{-3}$ .

Having found the dominant scattering contributions for the limit of low and high-carrier densities in the NWs, we now address the electrostatic screening length. Assuming first that the charge carriers in the NWs follow a 3D-type of behaviour over the entire  $N_d$  range, we determine the corresponding 3D Debye (screening) length,  $\lambda_D^{(3D)}$ , which is defined as [27]:

$$\lambda_D^{(3D)} = \sqrt{\frac{\epsilon_{NW}\epsilon_0 k_B T}{q^2 N_d}} \sim N_d^{-1/2} \quad (1)$$

where  $\epsilon_{NW} = 16$  is the dielectric constant of the NW material (assumed the same as for bulk Ge [28]),  $\epsilon_0$  the vacuum permittivity,  $k_B$  the Boltzmann constant,  $T$  the temperature and  $q$  the electron charge.

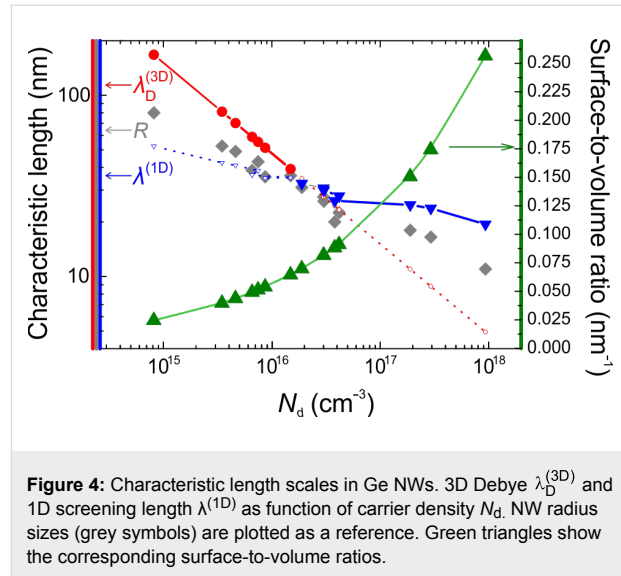
In Figure 4,  $\lambda_D^{(3D)}$  is plotted together with  $R$  as a function of  $N_d$ . For low-carrier densities,  $\lambda_D^{(3D)}$  is larger than the NW radius and shows a continuous decrease until it becomes comparable to  $R$  at about  $1$  to  $2 \times 10^{16} \text{ cm}^{-3}$ . From this point on  $\lambda_D^{(3D)} < R$ . However, a continued decrease in screening length would mean a reduction in the scattering cross-section, which is contradictory to the experimentally observed decrease in mobility (Figure 3b). Therefore this indicates that for higher  $N_d$  (smaller  $R$ ) a 3D description of the electrostatics in the NW is not suitable anymore and thus the screening length has to be described by a lower dimensional scenario. Since in a NW a 2D description of the charge carriers is not a reasonable approach, the 1D screening length  $\lambda^{(1D)}$  is better suited [29]. For our NWs, we can write

$$\lambda^{(1D)} = \sqrt{2 \frac{\epsilon_{NW}}{\epsilon_{ox}} R(N_d) t_{ox}} \sim N_d^{-1/6} \quad (2)$$

where  $\epsilon_{ox} \approx 7.44$  [27] is the dielectric constant of the native oxide,  $t_{ox} \approx 3 \text{ nm}$  (cf. Figure 1b) its thickness, and  $R(N_d)$  is the inverted  $N_d(R) \sim R^{-\alpha}$  (see above). That is, the screening length changes much slower with  $N_d$  compared to the 3D case.

Plotting  $\lambda^{(1D)}$  also in Figure 4 we find a seamless matching of  $\lambda^{(1D)}$  and  $\lambda_D^{(3D)}$  at about  $1$  to  $2 \times 10^{16} \text{ cm}^{-3}$  (equivalently  $R \approx 35$  to  $38 \text{ nm}$ ) which falls close to both the maximum in  $\mu_{NW}(N_d)$  and the entering into the slow varying regime of  $\sigma_{NW}(N_d)$  (Figure 3). We note that with increasing  $N_d$ ,  $\lambda^{(1D)}$  stays well above  $R$  which is consistent with the mobility decrease as well as the observed ionized impurity scattering dominating in this regime.

Considering the potential application of the Au-seeded Ge NWs for sensors, Figure 4 also reveals the most suitable range of



**Figure 4:** Characteristic length scales in Ge NWs. 3D Debye  $\lambda_D^{(3D)}$  and 1D screening length  $\lambda^{(1D)}$  as function of carrier density  $N_d$ . NW radius sizes (grey symbols) are plotted as a reference. Green triangles show the corresponding surface-to-volume ratios.

radii when plotting the surface-to-volume ratio also. Clearly, the quasi-1D regime is preferred as there the screening length is larger than  $R$  and the surface-to-volume ratio is maximised. In contrast, for radii  $\geq 37 \text{ nm}$ , the surface-to-volume ratio is by orders of magnitude lower, that is, not both prerequisites for an optimum sensor operation are met.

Summarizing, we demonstrated that the dominant scattering mechanisms and the electrostatic screening properties of Au-seeded VLS grown Ge NWs at room temperature are strongly dependent on their radius. Our results show that a crossover in charge carrier conduction occurs for carrier densities exceeding  $\approx 10^{16} \text{ cm}^{-3}$ , equivalent to the radius decreasing below approximately  $37 \text{ nm}$ . Analysis of the electrical screening properties shows that this is associated with a shift from a 3D to quasi-1D regime where the carrier drift is limited predominantly by ionized impurity scatterers. This suggests that Ge NWs only in the quasi-1D regime can be expected to deliver high-performance sensor capabilities.

## Supporting Information

### Supporting Information File 1

Extraction of intrinsic electrical transport parameters from measurement.

[<http://www.beilstein-journals.org/bjnano/content/supplementary/2190-4286-7-151-S1.pdf>]

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