

Supporting Information

for

Fingerprints of a size-dependent crossover in the dimensionality of electronic conduction in Au-seeded Ge nanowires

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Extraction of intrinsic electrical transport parameters from measurement

A. Nanowire conductivity

Nanowire resistance is measured in a four-point probe configuration, and is given by $R_{NW} = V_{4T} / I_d$ where V_{4T} is the voltage drop measured between the inner electrodes and I_d the current. For a NW of radius R , the *conductivity* is given by

$$\sigma_{NW} = \frac{1}{R_{NW}} \frac{L_C}{\pi R^2}, \quad (S1)$$

where L_C is the conduction channel length, defined as the distance between the outer edges of the four-point probe electrodes (cf. Ref [1] for more details).

B. Carrier mobility

Charge carrier mobility of the NWs was measured via the field-effect where the number of charges in the conduction channel is externally controlled by the applied gate voltage V_G . The electrical response of a NW device is quantified by its *extrinsic transconductance* g_m which is found from the sub-threshold slope of a transfer curve at fixed source-drain voltage V_{SD} :

$$g_m \equiv \left. \frac{\partial I_d}{\partial V_G} \right|_{V_{sd}}. \quad (S2),$$

The *intrinsic NW transconductance* can be obtained by decoupling the device-specific contact resistances R_C :

$$g_{in} = g_m \frac{1 + \frac{R_C}{R_{NW}}}{1 - g_m R_C / 2}, \quad (S3)$$

assuming that both source- and drain-electrode contact resistances are equivalent.

The contact resistance in turn is measured in two point configuration, where the total device resistance is given by: $R_{Tot} = R_{NW} + R_C$.

The *intrinsic mobility* can thus be found using the expression:

$$\mu_{NW} = \frac{g_{in}}{V_{SD}} \frac{L_C^2}{C}, \quad (S4),$$

where the capacitance C of the NW to the gate electrode is described by:

$$C = 2\pi\epsilon_{SiO_2}\epsilon_0 \frac{L_C}{\ln(t_{ox}/R)} \quad (S5)$$

with $t_{ox} = 300$ nm the SiO₂ thickness and ϵ_{SiO_2} its dielectric constant.

C. Carrier density

Carrier density can be calculated as:

$$N_d = \frac{\sigma_{NW}}{q\mu_{NW}} \quad (S6)$$

with q the electron charge.

Dominant doping from surface-states

Proof for the circumstance that we have doping which is dominated by the surface-states of the nanowire is seen by the following consideration:

We work with Au-seeded VLS Ge nanowires. From the entire synthesis process [2], one could assume that Au atom dopants – which would then be volume-dopants – provide the charge-carriers which we have measured in our experiments.

However, Au dopants in Ge are deep-level acceptors with an activation energy of the order of 100 to 200 meV (e.g. [3-5]). That is, their ionisation probability at room temperature (our experimental condition) would be below 1%. Considering our experimentally measured carrier densities between 10^{15} to 10^{18} cm^{-3} , we would have 10^{17} to 10^{20} cm^{-3} Au-atom density in the Ge nanowires. This large amount of Au atoms however has not been detected in TEM of our nanowires (cf. Figure 1b; [2]) but would have been easily detectable by TEM techniques (see e.g. [6,7])

Weak switching behaviour of Ge NWs (transfer characteristics)

The poor switching behaviour is typical for VLS synthesized Ge NWs and is a consequence of the generally high doping of the NWs through surface states up to 10^{18} cm^{-3} (several orders of magnitude higher than intrinsic Ge).

Supplementary References:

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5. Chapter 5 in: Egerton, *Electron Energy-Loss in the Electron Microscope*, Ch. 5
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